MATH 1136 FINAL REVIEW

BASIC GEOMETRIC CONCEPTS AND REASONING

- lines, planes
- angles
- the parallel postulate
- polygons (mainly triangles and quadrilaterals)
- circles, spheres
- angle sum by walking/turning and parallel postulate
- compass/straightedge constructions
- reasoning about properties of polygons: simple proofs, Venn diagrams

Suggestions from the *Practice Exercises* (Orange)

ALGEBRAIC EXPRESSIONS

- algebraic expressions from pictures and vice versa
- expressions and equations to describe relationships among quantities
- solving equations
- strip diagrams as a bridge between written descriptions and algebraic expressions

Suggestions from the *Practice Exercises* (Orange)

 $\begin{array}{l}9.1.5,\,9.1.6,\,9.2.2,\,9.2.5,\,9.3.1,\,9.3.3,\,9.3.4,\,9.4.4,\,9.5.1,\\9.5.2,\,9.5.3\end{array}$

Functions

- key (defining) property of functions
- using reasoning with remainders to understand repeating sequences
- arithmetic and geometric sequences
- shape of graph and qualitative behavior of function
- proportional relationships as linear functions
- arithmetic sequences as linear functions
- equations for linear functions

Suggestions from the *Practice Exercises* (Orange)

9.6.1, 9.6.2, 9.6.3, 9.6.5, 9.7.4, 9.7.6, 9.8.2, 9.8.3, 9.8.4

Measurement topics

- Fundamentals of measurement
 - meaning of measurement
 - measurable v.s. non-measureable attributes
 - units
- Length, area, volume
 - similarities and differences between the three
- Error and precision in measurement
- Dimensional analysis

Area topics (Part I)

- Area of rectangles
 - meaning of area
 - length x width
- Moving and additivity principles
- Areas of triangles

Suggestions from the *Practice Exercises* (Orange)

AREA TOPICS (PART II)

- Areas of triangles, parallelograms
- Cavalieri's principle
- square constant and circle constant
- Circle area, estimates of pi and tau
- Areas of irregular shapes
- The Pythagorean theorem

Suggestions from the Practice Exercises (Orange)

 $\begin{array}{l} 12.5.1,\ 12.5.2,\\ 12.6.1,\ 12.6.2,\ 12.6.3,\ 12.6.4,\ 12.6.5,\\ 12.7.2,\ 12.8.2,\ 12.8.3,\\ 12.9.1,\ 12.9.2,\ 12.9.5,\ 12.9.6,\ 12.9.7,\ 12.9.8,\ 12.9.9\end{array}$

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VOLUME TOPICS

- Meaning of volume; volumes of prisms.
- Faces, Edges, Vertices of basic 3D shapes.
- Meaning of surface area.
- Patterns for cones and pyramids. Relationships between measurements of the pattern and measurements of the 3D shape.
- Cross sections of 3D shapes.
- Cavalieri's principle. If two shapes have the same cross-section area at every height, then they have the same volume. Explain how the shearing version of Cavalieri's principle (presented in the text) is a special case of this.
- Volume of cone/pyramid is $\frac{1}{3}$ the volume of the cylinder/prism with the same base and height. This leads to the volume formula for circular cones and rectangular pyramids.
- Volume of a sphere is $\frac{4}{3}\pi r^3$. The $\frac{4}{3}$ comes from comparison with a cylinder and two cones.

Suggestions from the *Practice Exercises* (Orange)

13.1.1, 13.1.2

13.2.2, 13.2.3, 13.2.4, 13.2.7, 13.2.8 13.3.2, 13.3.3, 13.3.4, 13.3.8 13.4.2, 13.4.3

TRANSFORMATIONS, CONGRUENCE, AND SIMILARITY TOPICS

- Transformations in the plane
 - Four main types of isometry: rotation, reflection, translation, glide reflection (a.k.a. "trans-flection").
 - Important non-isometries: shearing, scaling.
- Symmetry, congruence
 - Types of symmetry
 - Triangle congruence
 - Other congruence and geometric properties of compass/straightege constructions
- Similarity (scaling)
 - Relating similarity problems to ratio problems
 - Concept of similarity and slope of a line
 - Triangle similarity
- Scaling area and volume
 - Linear, area, and volume scale factors
 - Variety of applications

Suggestions from the *Practice Exercises* (Orange)

 $\begin{array}{l} 14.1.1, \ 14.1.2, \ 14.1.3\\ 14.2.1, \ 14.2.2, \ 14.2.3, \ 14.2.4,\\ 14.3.1, \ 14.3.2, \ 14.3.3,\\ 14.4.1, \ 14.4.2,\\ 14.5.3, \ 14.5.4, \ 14.5.5,\\ 14.6.2, \ 14.6.3\end{array}$

Probability

- Key principles of probability
- Theoretical v.s. empirical probabilities
- Counting techniques
 - counting combinations
 - counting choices
- Probabilities and fraction arithmetic
- Probabilities of multistage/compound events

Suggestions from the *Practice Exercises* (Orange)

 $\begin{array}{l} 16.1.1,\ 16.1.2,\ 16.2.2,\ 16.2.4,\ 16.2.5,\\ 16.3.1,\ 16.3.2,\ 16.3.3,\ 16.3.4,\ 16.4.1,\ 16.4.2,\ 16.4.3\end{array}$