

**A.1 Shelby and Scotty**

Shelby and Scotty want to express the number 27 in base 4. However, they used very different methods to do this. Let's check them out.

**A.1.1)** Consider Shelby's work:

*6 groups of 4*  

$$\begin{array}{r} 6 \\ 4 \overline{)27} \end{array} \text{ R3} \quad \begin{array}{r} 1 \\ 4 \overline{)6} \end{array} \text{ R2} \quad \begin{array}{r} 0 \\ 4 \overline{)1} \end{array} \text{ R1} \quad \Rightarrow \quad \begin{array}{|c|} \hline 123 \\ \hline \text{ABC} \\ \hline \end{array}$$

*1 group of 4*  
*4 groups of 4*

- (a) Describe how to perform this algorithm.
- (b) Provide an additional relevant and revealing example demonstrating that you understand the algorithm.

**A.1.2)** Consider Scotty's work:

*4<sup>3</sup>*  

$$\begin{array}{r} 0 \text{ R27} \\ 4^3 \overline{)27} \end{array} \quad \begin{array}{r} 1 \text{ R11} \\ 4^2 \overline{)27} \end{array} \quad \begin{array}{r} 2 \text{ R3} \\ 4 \overline{)11} \end{array} \quad \Rightarrow \quad \begin{array}{|c|} \hline 123 \\ \hline \text{ABC} \\ \hline \end{array}$$

- (a) Describe how to perform this algorithm.
- (b) Provide an additional relevant and revealing example demonstrating that you understand the algorithm.

**A.1.3)** Create an illustration (or series of illustrations) based on the 27 marks below that models Shelby's method for changing bases.



Further, explain why Shelby's method works.

**A.1.4)** Create an illustration (or series of illustrations) based on the 27 marks below that models Scotty's method for changing bases.



Further, explain why Scotty's method works.